



Bell test using NV-centers

Local Realism

- **Local**

Physical influences can't propagate faster than light

- **Realism**

Physical properties are defined before and independent of measurement

- **CHSH Bell test**

Gives us an inequality $S \leq 2$ that holds under local realism

- Inequality violated in many experiments → our world is QM!

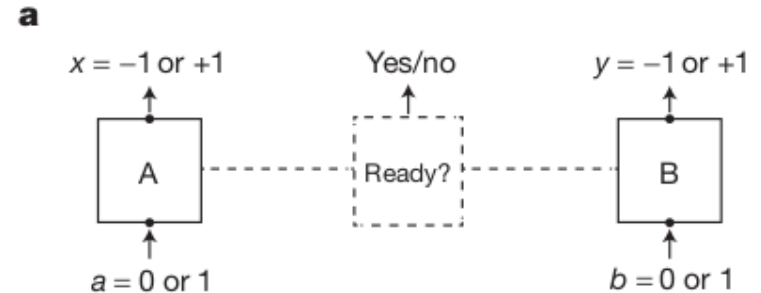
Basic experiment

- **For each trial**

- Entangle Spins in Box A and B
- Measure Spins
 - $a=0 \rightarrow Z$ measurement in Box A
 $a=1 \rightarrow X$ measurement in Box A
 - $b=0 \rightarrow (-Z + X)/\sqrt{2}$ measurement in Box B
 $b=1 \rightarrow (-Z - X)/\sqrt{2}$ measurement in Box B

- **Evaluate CHSH inequality**

- $S = |\langle \mathbf{x} \cdot \mathbf{y} \rangle_{(0,0)} + \langle \mathbf{x} \cdot \mathbf{y} \rangle_{(0,1)} + \langle \mathbf{x} \cdot \mathbf{y} \rangle_{(1,0)} - \langle \mathbf{x} \cdot \mathbf{y} \rangle_{(1,1)}|$
 $\rightarrow \langle \mathbf{x} \cdot \mathbf{y} \rangle_{(a,b)}$ expectation value for input bits a and b
- QM predicts $S = 2\sqrt{2}$
- Problem: **Loopholes!** \rightarrow **Need Event-Ready signal**



Hensen et. al.

Locality Loophole

Locality condition:

- signals travel with $v \leq c$
- two boxes A and B are separated s.t. a signal from A cannot arrive at B before the output value of B has been recorded

Problem:

- possible communication between the two boxes

→ this leads to locality loophole

Solution:

- spatial separation of 1.3 km between the boxes
- distance between pair of photons long enough to address locality loophole using fast setting changes

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Detection Loophole

Problem:

- We need to exclude erroneous output bits x and y for assuming «fair sampling»

Solution:

- Check that entanglement was successful and record Event-Ready signal
- Spin read-out is measured very efficiently

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Simultaneously closing both loopholes

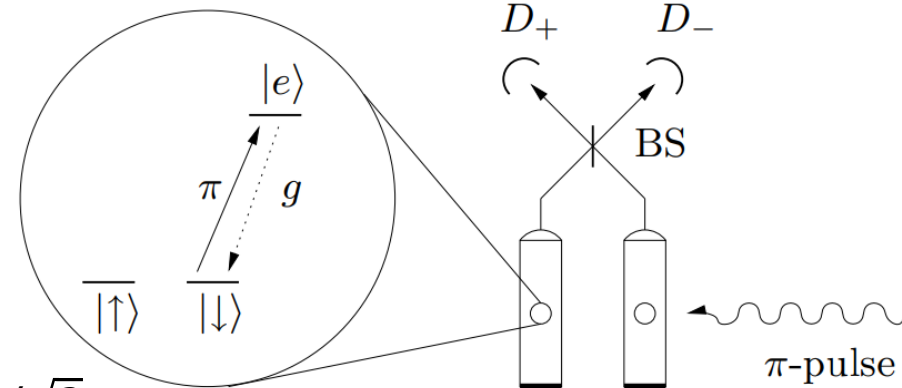


- Spatial separation of 1280 m between the qubits at locations A, B
- Record Event-Ready signal at location C

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Entangling distant NV centers

- Optical π -Pulse induces transition (selection rule)
 - $|\downarrow\rangle \rightarrow |e\rangle$
 - $|\uparrow\rangle \rightarrow |\uparrow\rangle$
- Scheme
 - 1) Initialize both qubits to $(|\uparrow\rangle + |\downarrow\rangle)/\sqrt{2}$
 - 2) To both apply a π -Pulse
 - 3) Wait for some time t for an event at D_{\pm} ($|e\rangle \rightarrow |\downarrow\rangle$ emits photon)
 - 4) Apply SWAP operation to both qubits
 - 5) Repeat steps 2-4
- If we detect exactly one photon each round
 - get max. entangled state $(|\downarrow\uparrow\rangle \pm |\uparrow\downarrow\rangle)/\sqrt{2}$
 - **Event ready signal**
- Beam splitter erases which-path information



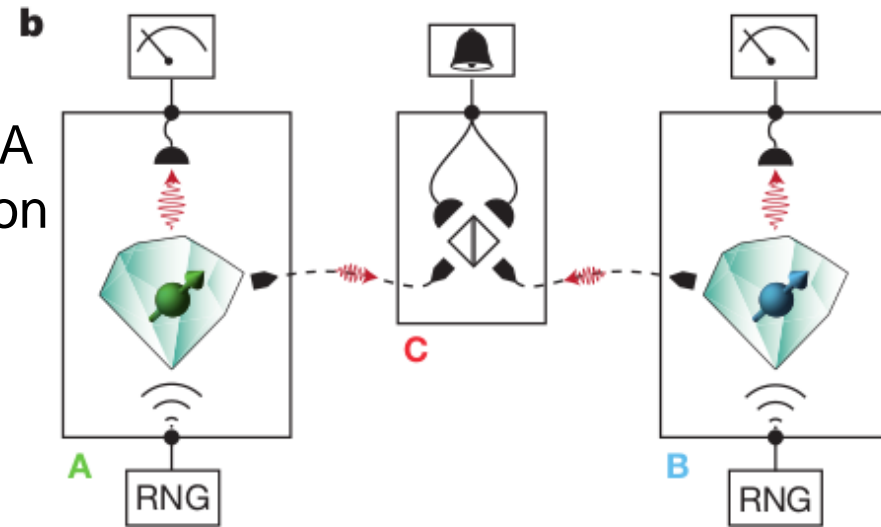
Don't confuse:
This is not the π -Pulse on the Bloch-Sphere!

Barrett et. al.

Experimental setup

- Entangle NV centers at locations A and B and send photons to location C → Record event ready signal
- RNG generates the input bit a (or b) to choose random basis
→ rotate spins accordingly
- Optical readout (Z measurement)
 $m_s = 0 \equiv |\uparrow\rangle \rightarrow x, y = +1$
 $m_s = \pm 1 \equiv |\downarrow\rangle \rightarrow x, y = -1$

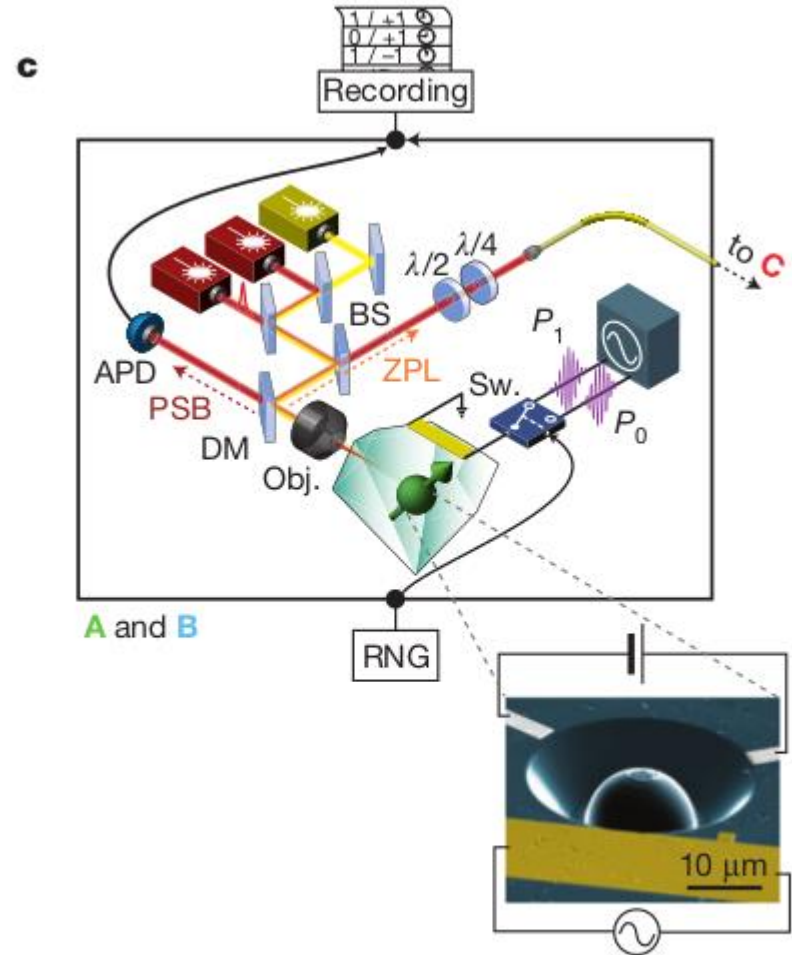
As before only $m_s = 0$ state is excited → dark & bright state



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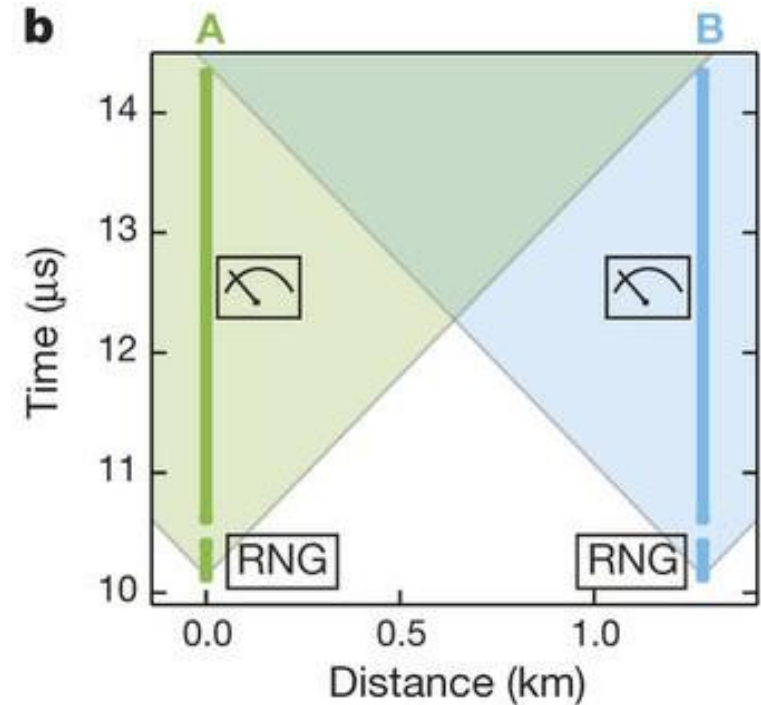
Detailed Setup at locations A,B

- **DM**: Dichroic mirror allows separation into a off-resonant part (ZPL) and a resonant part (PSB)
- **Sw**: Selects predefined MW-pulses P_0 , P_1 for basis selection
- **APD**: Single-photon counter
→ confocal microscope



Space-time analysis

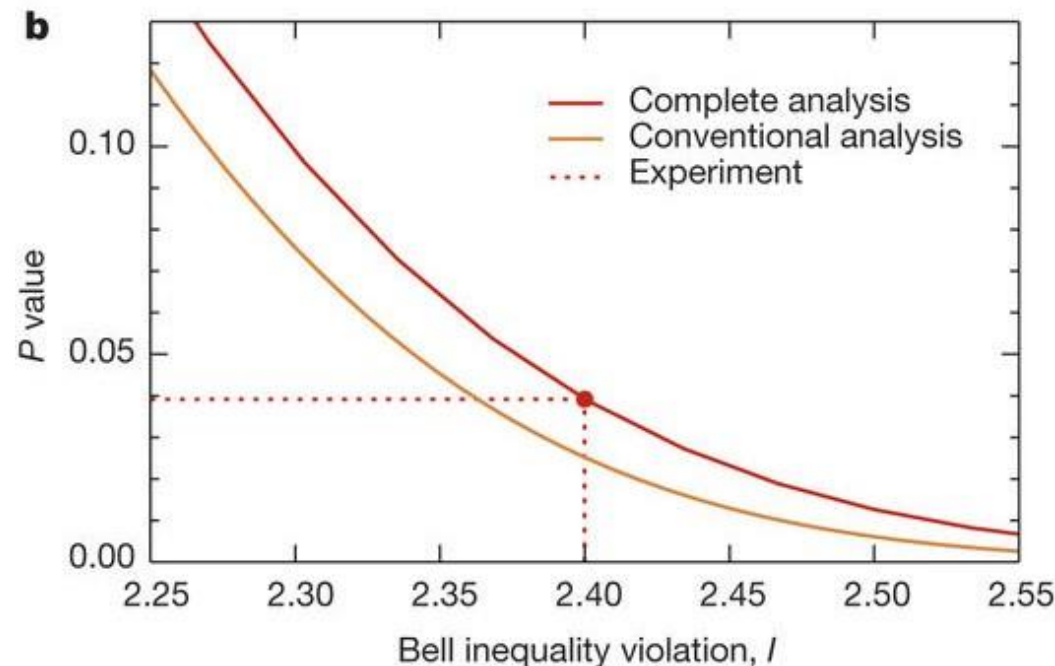
- spin separation: 1'280 km
→ **4.27 μs** separation between local events at A and B
- random basis choice: **160 ns**
- read-out duration: **3.7 μs**
- uncertainty in distance between the laboratories: **90 ns**
- initialisation and single-shot read-out fidelity:
 - for A: **97.1%**
 - for B: **96.3%**
- fidelity of ideal state Y: **92%**



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Results

- Entanglement success probability: 6.4×10^{-9}
→ 1 event-ready signal per hour
- 245 trials were performed over 220 hours
- expected value:
 $S = 2.30 \pm 0.07$
- theoretically maximum value: $S = 2\sqrt{2} \approx 2.83$
- found value:
 $S = 2.45$



“Conventional” Analysis

Assumptions:

- Bell trials are independent of each other
- random input have zero predictability
- outcome follows Gaussian distribution

→ standard deviation of **0.20** for S

→ **P = 0.019**

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“Complete” Analysis

Assumption:

- random input have partial predictability

→ **P = 0.039**

Lookout:

- for 700 trials and $S = 2.4$ one could get $P = 0.001$

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Final Comments

- The experiment violates the CHSH inequality
→ reject local-realist theories
- It was the first test that simultaneously closed the detection AND the locality loophole
- Central idea: Entangle distant NV centers with photons by using an Event-Ready scheme